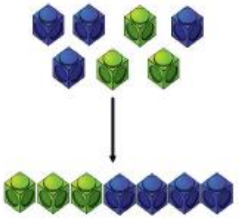
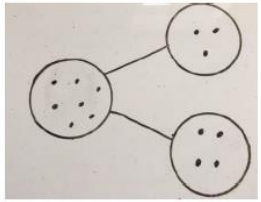
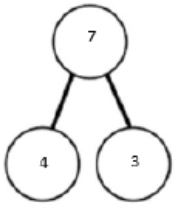
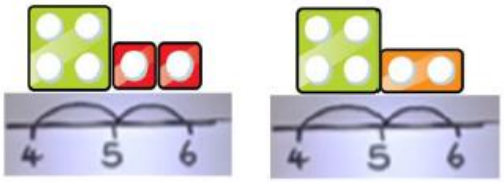
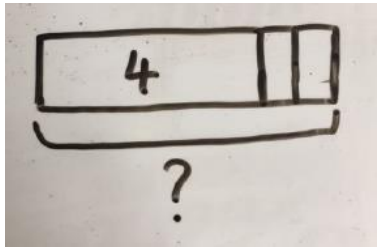
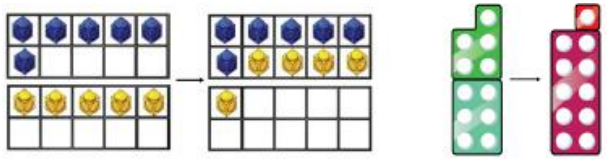
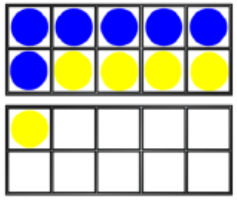
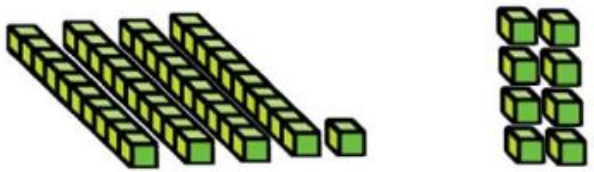
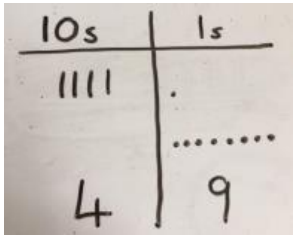
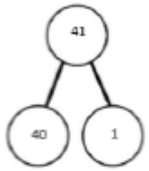
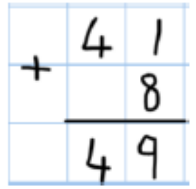
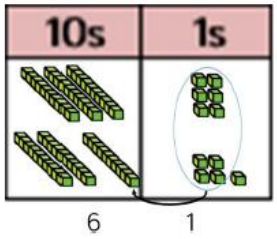
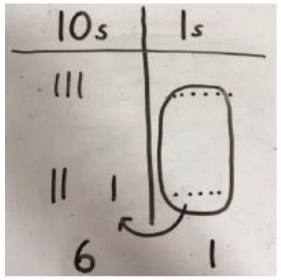
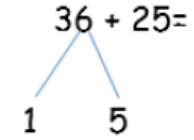
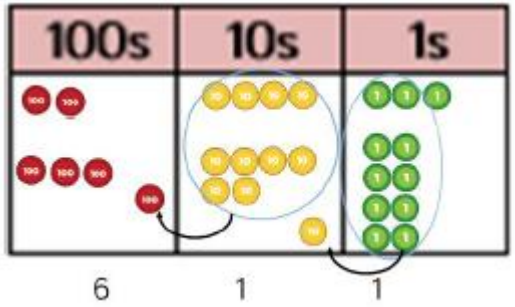
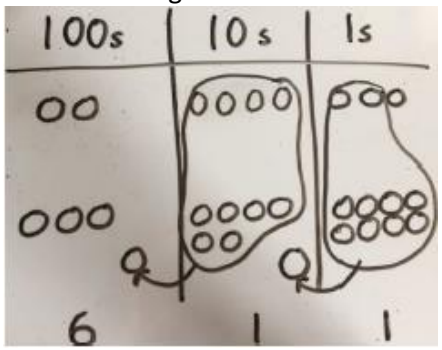
Radcliffe Hall CE/Methodist Primary School

Calculation Policy

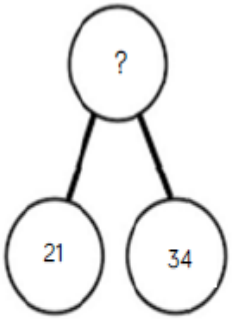
Calculation: Addition

Key Vocabulary: sum, total, parts and wholes, plus, add, altogether, more, is equal to, is the same as			
Stage	**Concrete**	**Pictorial**	**Abstract**
1	**Combining two parts to make a whole** (use other resources too e.g. shells, eggs, teddy bears). 	Children to represent the cubes using dots or crosses. They could put each part on a part whole model too. 	4 + 3 = 7 Four is a part, three is a part and the whole is seven. 
2	**Counting on using number lines**, using cubes or Numicon.  	A bar model which encourages the children to count on, rather than count all. 	The abstract number line: What is 2 more than 4? What is the total of 4 and 2? 4 + 2 
3	**Regrouping to make 10;** using ten frames and counters/cubes or Numicon. 6 + 5 	Children to draw the ten frame and counters/cubes. 	Children to develop an understanding of equality e.g. $6 + \square = 11$ $6 + 5 = 5 + \square$ $6 + 5 = \square + 4$

4	**TO + O using base 10.** Continue to develop understanding of partitioning and place value. 41 + 8 	Children to represent the base 10 e.g. lines for tens and dot/crosses for ones. 	41 + 8  1 + 8 = 9 40 + 9 = 49 
5	**TO + TO using base 10.** Continue to develop understanding of partitioning in place value. 36 + 25 	Children to represent the base 10 in a place value chart. 	Looking for ways to make 10.  30 + 20 = 50 5 + 5 = 10 50 + 10 + 1 = 61 36 Formal method: +25 61 1
6	**Use of place value counters to add HTO + TO, HTO + HTO etc.** When there are 10 ones in the 1s column, we exchange for 1 ten, when there are 10 tens in the 10s column, we exchange for 1 hundred. 	Children to represent the counters in a place value chart, circling when they make an exchange. 	243 +368 611 1 1

Conceptual Variation

Different ways to ask children to solve 21 + 34



?	
21	34

Word problems:
In year 3, there are 21 children and in year 4, there are 34 children.
How many children in total?

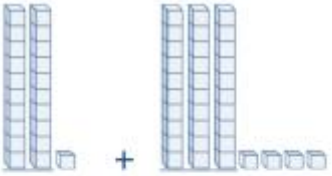
21 + 34 = 55. Prove it

21
+34
——

21 + 34 =

☐ = 21 + 34

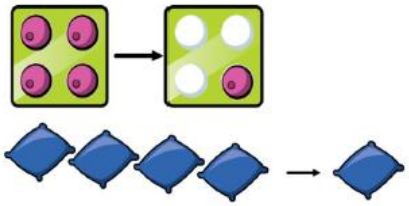
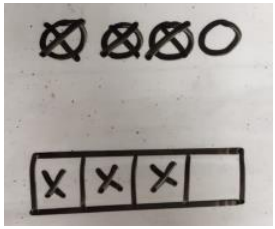
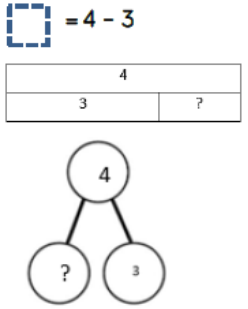
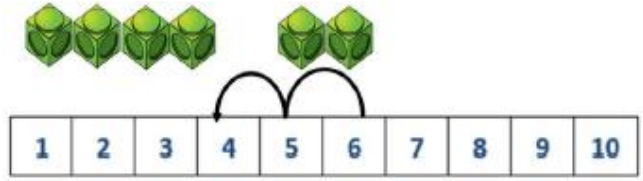
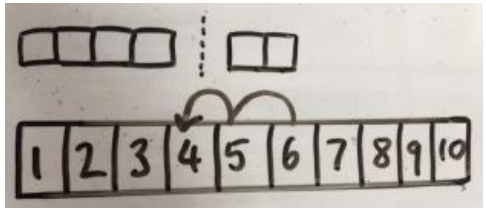
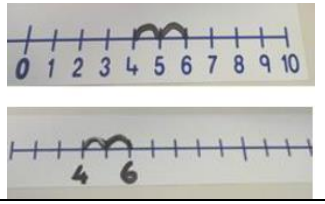
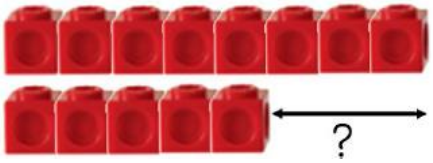
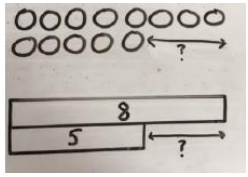
Calculate the sum of twenty-one and thirty-four.

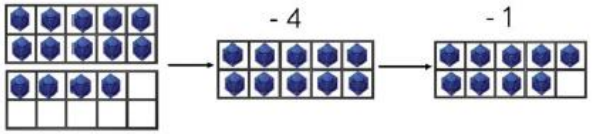
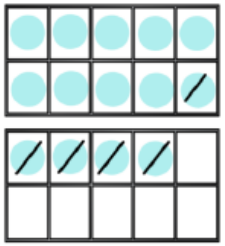
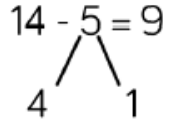
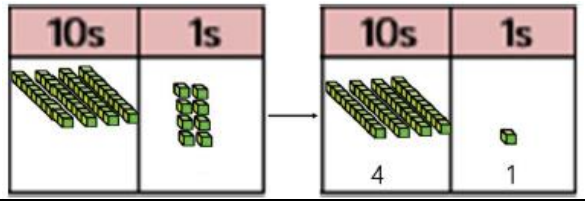
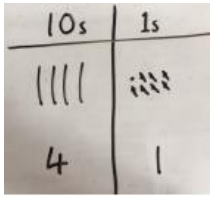
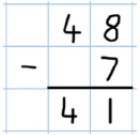
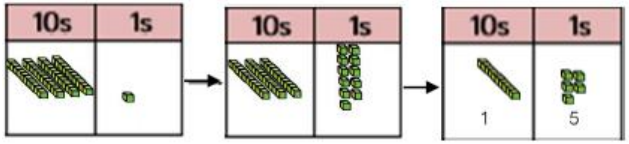
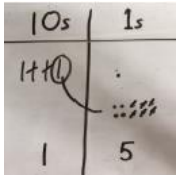
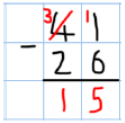
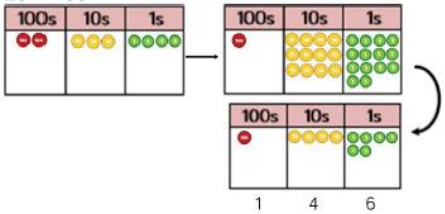
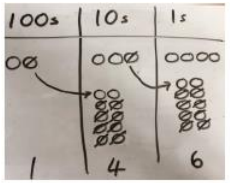
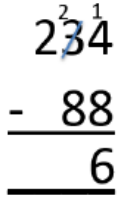


Missing digit problems:

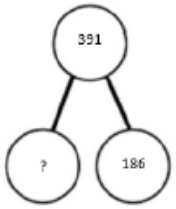
10s	1s
10 10	1
10 10 10	?
?	5

Calculation: Subtraction

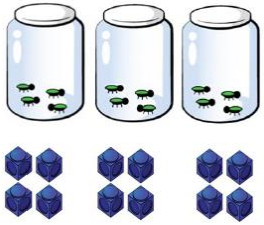
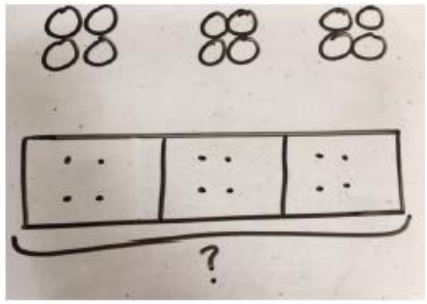
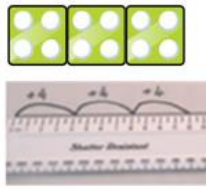
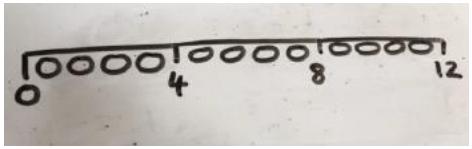
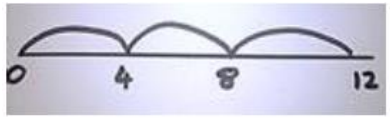
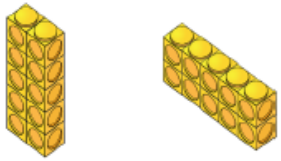
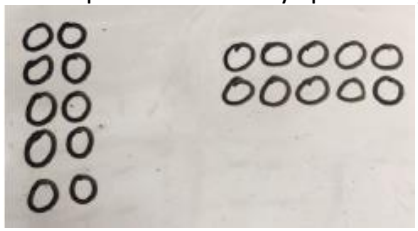
Key Vocabulary: take away, less than, the difference, subtract, minus, fewer, decrease			
Stage	**Concrete**	**Pictorial**	**Abstract**
1	**Physically taking away and removing objects from a whole** (ten frames, Numicon, cubes and other items such as beanbags could be used). 4 – 3 = 1 	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used. 	4 – 3 = 
2	**Counting back** (using number lines or number tracks) children start with 6 and count back 2. 6 – 2 = 4 	Children to represent what they see pictorially. 	Children to represent the calculation on a number line or track and show their jumps. 
3	**Finding the difference** (using cubes, Numicon or other objects). Calculate the difference between 8 and 5. 	Children to draw the concrete materials they have used or use the bar model to illustrate what they need to calculate. 	Find the difference between 8 and 5. 8 – 5, the difference is ☐ Children to explore why 9 - 6 = 8 – 5 = 7 – 4 have the same difference.

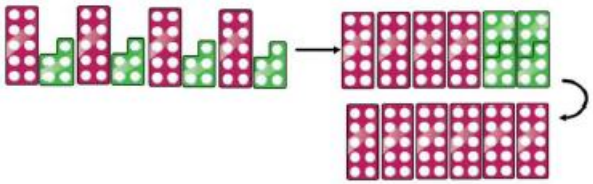
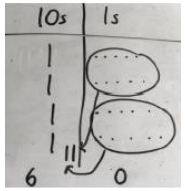
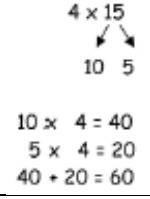
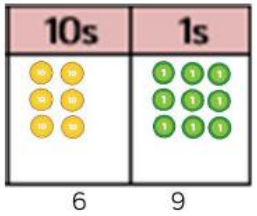
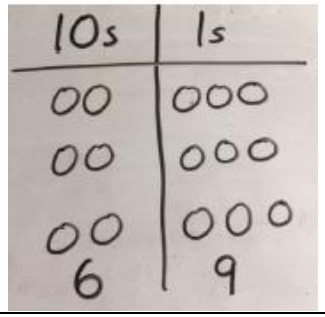
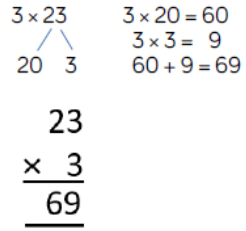
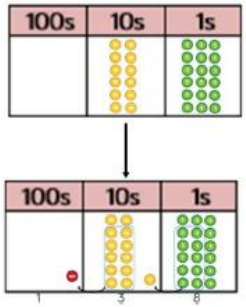
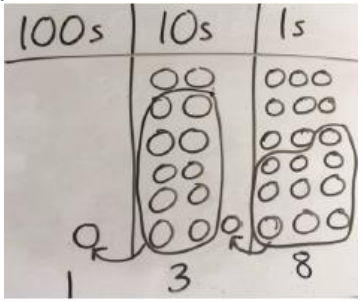
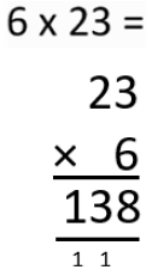
4	**Making 10** using ten frames 14 - 5 	Children to present the ten frame pictorially and discuss what they did to make 10. 	Children to show how they can make 10 by partitioning the subtrahend.  14 – 4 = 10 10 – 1 = 9
5	**Column method** using base 10. 48 - 7 	Children to represent the base 10 pictorially. 	Column method or children could count back 7. 
6	**Column method** using base 10 and having to exchange. 41 – 26 	Represent the base 10 pictorially, remembering to show the exchange. 	Formal column method. Children must understand that when they have exchanged the 10, they still have 41 because 41 = 30 + 11. 
7	**Column method** using place value counters 234 – 88 	Represent the place value counters pictorially; remembering to show what has been exchanged. 	Formal column method. Children must understand what has happened when they have crossed out digits. 

Conceptual Variation

Different ways to ask children to solve 391 - 186			
 391 186 | ?	Raj spent £391, Timmy spent £186. How much more did Raj spend? Calculate the difference between 391 and 186.	□ = 391 – 186 391 -186 ___ What is 186 less than 391?	Missing digit calculations 3 9 □ - □ □ 6 □ 0 5

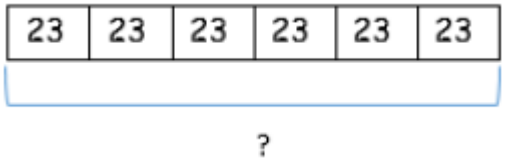
Calculation: Multiplication

Key Vocabulary: double, times, multiplied by, the product of, groups of, lots of, equal groups.			
Stage	**Concrete**	**Pictorial**	**Abstract**
1	**Repeated grouping/repeated addition.** 3 x 4 4 + 4 + 4 There are 3 equal groups, with 4 in each group. 	Children to represent the practical resources in a picture and use a bar model. 	3 x 4 = 12 4 + 4 + 4 = 12
2	**Number lines to show repeated groups** 3 x 4 	Represent this pictorially alongside a number line e.g.: 	Abstract number line showing three jumps of four. 3 x 4 = 12 
3	**Use arrays to illustrate commutativity** (counters and other objects can be used too). 2 x 5 = 5 x 2 	Children to represent the arrays pictorially. 	Children to be able to use an array to write a range of calculations e.g. 10 = 2 x 5 5 x 2 = 10 2 + 2 + 2 + 2 + 2 = 10 10 = 5 + 5

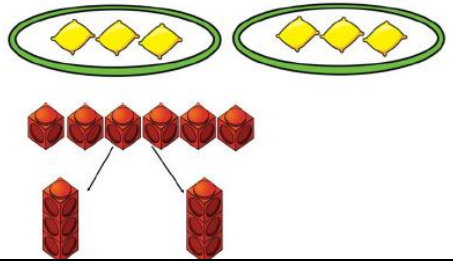
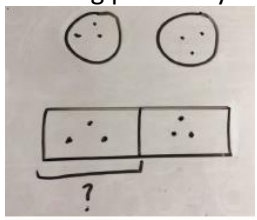
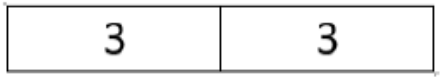
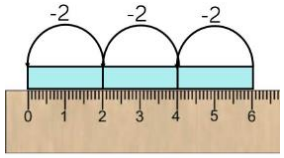
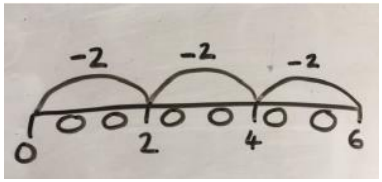
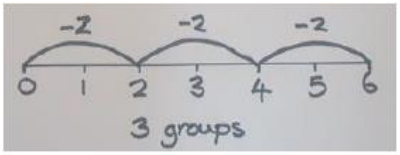
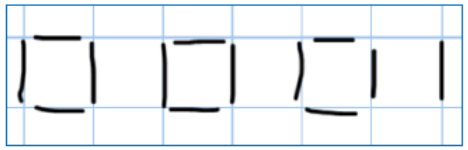
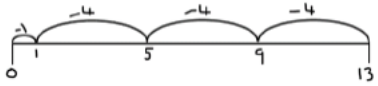
4	**Partition to multiply** using Numicon and base 10. 4 x 15 	Children to represent the concrete manipulatives pictorially. 	Children encouraged to show the steps they have taken. 
5	**Formal column method** with place value counters or base 10. 3 x 23 	Children to represent the counters pictorially. 	Children to record what it is they are doing to show understanding. . 
6	**Formal column method with place value counters.** 6 x 23 	Children to represent the counters/base 10, pictorially. 	Formal written method. 
7	**When the children start to multiply 3d x 3d and 4d x 2d etc., they should be confident with the abstract.** To get 744 children have solved 6 x 124. To get 2480 they have solved 20 x 12.		Formal column method. Children must understand what has happened when they have crossed out digits.

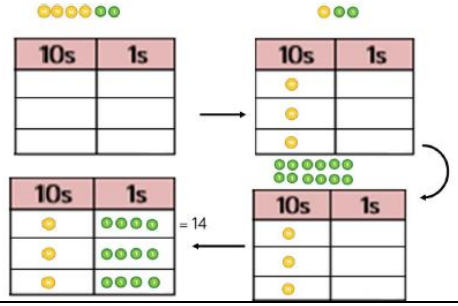
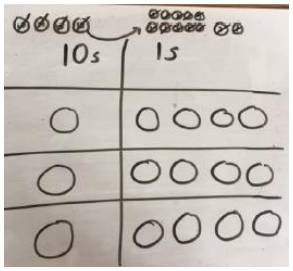
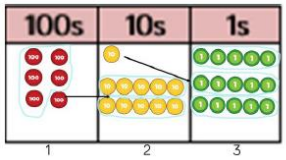
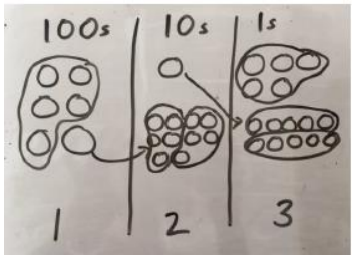
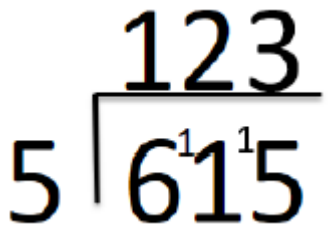
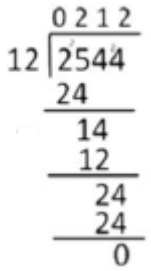
Conceptual Variation

Different ways to ask children to solve 23 x 6

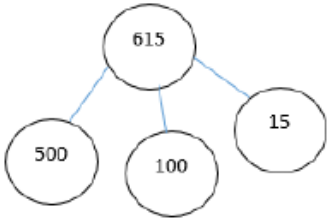
	Mai had to swim 23 lengths, 6 times a week. How many lengths did she swim in one week? With the counters, prove that 6 x 23 = 138	Find the product of 6 and 23 $6 \times 23 =$ $\square = 6 \times 23$ $\begin{array}{r} 6 \\ \times\ 23 \\ \hline \end{array}$ $\begin{array}{r} 23 \\ \times\ 6 \\ \hline \end{array}$	What is the calculation? What is the product? 

Calculation: Division

Key Vocabulary: half, share, group, divide, divided by.			
Stage	**Concrete**	**Pictorial**	**Abstract**
1	**Sharing** using a range of objects. 6 ÷ 2 	Represent the sharing pictorially. 	Children encouraged to use their 2 times tables facts. 6 ÷ 2 = 3 
2	**Repeated subtraction** using rods above a ruler or number line. 6 ÷ 2  3 groups of 2	Children to represent repeated subtraction pictorially. 	Abstract number line to represent the equal groups that have been subtracted. 
3	**2d ÷ 1d with remainders** using lollipop sticks. 13 ÷ 4 Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.  There are 3 whole squares, with 1 left over.	Children to represent the lollipop stick pictorially. There are 3 whole squares, with 1 left over. 	13 ÷ 4 = 3 remainder 1 Children should be encouraged to use times table facts; they could also represent repeated addition on a number line. 

4	**Sharing using place value counters.** 42 ÷ 3 = 14 	Children to represent the place value counters pictorially. 	Children to be able to make sense of the place value counters and write calculation to show the process. 42 ÷ 3 42 = 30 + 12 30 ÷ 3 = 10 12 ÷ 3 = 4 10 + 4 = 14
5	**Short division** using place value counters to group. 615 ÷ 5  1. Make 615 with place value counters. 2. How many groups of 5 hundreds can you make with 6 hundred counters? 3. Exchange 1 hundred for 10 tens. 4. How many groups of 5 tens can you make with 11 ten counters? 5. Exchange 1 ten for 10 ones. 6. How many groups of 5 ones can you make with 15 ones?	Children represent the place value counters pictorially. 	Children to calculate using the short division scaffold. 
6	**Long division** 2544 ÷ 12 		

Conceptual Variation

Different ways to ask children to solve 615 ÷ 5			
Using the part whole model below, how can you divide 615 by 5 without using short division?  	I have £615 and share it equally between 5 bank accounts. How much will be in each account? 615 pupils need to be put into 5 groups. How many will be in each group?	$5 \overline{)615}$ $615 \div 5 =$ $\square = 615 \div 5$	What is the calculation? What is the answer?